

St. John's Primary School Calculation Policy Spring 2016

Y1 - Y6

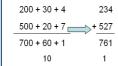
St. John's Primary School – Calculation Policy 2016

Introduction and rationale

The St. John's Primary School Calculation Policy has been written with the involvement of all staff to support the implementation of the new National Curriculum (2013). A document for each operation addresses what and how to teach year by year. The policy lays out expectations for both mental and written calculations (generally collated for Key Stage 1), including calculation of fractions, and includes statements from the national curriculum and supplementary guidance as below:

- National Curriculum statutory statements in bold
- National Curriculum non-statutory guidance in italics
- Additional/Supplementary guidance plain text







3 x 5

Orange boxes provide teaching guidance and tips, whilst speech bubbles denote examples either of key questions $\frac{1}{2}$ ask or of children's thinking/ speaking. A vocabulary list is provided to encapsulate suggested vocabulary for each year group. This is not exhaustive. See 'Mathematics glossary for teachers in Key stages 1 to 3' on the NCETM https://www.ncetm.org.uk/ resources/42990#glossary.

Representations



Key to successful implementation of a school calculation policy is consistent use of representations (model and images that support conceptual understanding of the mathematics) and this policy promotes a range of relevant representations, across the primary years. Mathematical understanding is developed through use of representations that are first of all concrete (e.g. Numicon, Dienes apparatus), and then pictorial (e.g. Array, place value counters) to then facilitate abstract working (e.g. Columnar addition, long multiplication). This

policy guides teachers through an appropriate progression of representations, and if at any point a pupil is struggling they should revert to familiar pictorial and/or concrete materials/ representations as appropriate. Whilst a mathematically fluent child will be able to choose the most appropriate representation and procedure to carry out a calculation, whether written or mental, schools should support pupils with carefully selected representations that underpin calculation methods (as detailed in this policy), and ensure there is consistency across year groups. The 'Representations to support mental and written calculation' box on each page provides a range of models and images that underpin calculating in that year group. It is not an exhaustive collection, and applies to both mental and written calculation in most circumstances. Additional specific examples are included inside mental and written calculation boxes.

Progression in Calculation

The St. John's Primary School calculation policy promotes particular methods and procedures with particular representations alongside to support understanding of calculation, in order to meet requirements (use of columnar methods from Year 3 onwards for all four operations, including long multiplication and long division in Year 5/6). It is recommended that schools ensure consistency in both procedure and conceptual understanding to ensure fluency and confidence with written methods. This policy guides schools in progression for each operation to ensure smooth transition. It is important that conceptual understanding, supported by the use of representations, is secure for procedures, and if at any point a pupil is struggling with a procedure, they should revert to concrete and/or pictorial resources and representations to solidify understanding.

| videos to support matnematical teaching and learning | | | | |
|---------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------|--------------------------------------------|--|
| Multiplication | Algebra | Number facts | Division | |
| https://www.ncetm.org.uk/resources/40530 | https://www.ncetm.org.uk/ | https://www.ncetm.org.uk/ | https://www.ncetm.org.uk/ | |
| KS1 - Multiple Representations of | resources/43649 | resources/40533 | resources/43589 | |
| Multiplication | KS1 - Look at 'missing numbers' | KS1 - Number bonds to ten | KS1- Sharing and grouping | |
| KS1- The commutative law for multiplication | KS2 - Equations and substitution | KS1 - Consolidation and practice (Addition | KS 2 - Place value counters for | |
| Lower KS2 - Grid multiplication as an interim | KS3 - Factorising* | and Subtraction) | division | |
| step | | KS1 - Reinforcing Table Facts | KS 3 - Group working on | |
| Upper KS2 - Moving from grid to a column | | KS1 - Rapid recall of multiplication facts | problems* | |
| Number and Place value | Fractions | Subtraction | Multiplicative | |
| https://www.ncetm.org.uk/resources/40534 | https://www.ncetm.org.uk/ | https://www.ncetm.org.uk/ | reasoning | |
| KS1 - Counting in steps of one and ten | resources/43609 | resources/40532 | https://www.ncetm.org.uk/ | |
| KS1 - Partitioning in different ways | KS1 - Adding fractions and mixed | Lower KS2 – Partitioning | resources/43669 | |
| KS1 - Addition and Subtraction | numbers | Lower KS2 - Discussing Subtraction | KS2 - Bar model for | |
| | | | | |
| KS1 - Using resources to develop fluency and | KS2 - Using an array to add fractions | Strategies | multiplication | |
| KS1 - Using resources to develop fluency and understanding KS2 - Partitioning (subtraction) | KS2 - Using an array to add fractions KS2 - Bar model dividing by fractions KS3 - Fraction wall to add fractions* | Strategies Lower KS2 - Developing Column Subtraction Upper KS2- Column Subtraction | multiplication KS3 - Ratio and proportion* | |

Mental Calculations

- •Read, write and interpret mathematical statements using symbols +, -, =
- •Represent and use number bonds and related addition facts within 20
- •Add one digit and two-digit numbers up to 20, including zero.
- •Solve one-step problems using concrete objects and pictorial representations, and missing number problems such as $7 = \Box 9$
- •Given a number, identify (and use the language) one more

Written Calculations

- •Begin to compare (what's the same/different?) for commutative sums e.g 3 + 7 = 7 + 3
- •Memorise and reason with number bonds to 10 & 20 in several forms
- Add using objects, Numicon, cubes etc and number lines and tracks
- Check with everyday objects
- •Ensure pre-calculation steps are understood, including:
 - •Counting objects (including solving simple concrete problems
 - •Conservation of number:
 - •Recognise place value in numbers beyond 20
 - Counting as reciting and as enumerating





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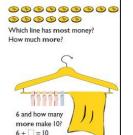
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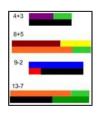
2 3

Use a range of concrete and pictorial representations, including:

Representations to support mental and written calculations.

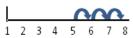
Links from other strands

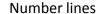
















Bead strings



Number tracks



Real everyday objects



- Combine and increase numbers, counting forwards and backwards.
- Develop the concept of addition and subtraction and ... use these operations flexibly.
- Discuss and solve problems in familiar practical contexts, including using quantities
- Compare, describe and solve practical [measure] problems e.g. longer, more than, heavier than
- Problems terminology should include: put together, add, altogether, total, take away, distance between, difference between, more than and less than.

Calculations Mental Add numbers using concrete objects, pictorial representations, and mentally, including:

- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers
- adding three one-digit numbers
- Recall and use addition and subtraction facts to 20 facts fluently, and derive and use related facts up to 100

17 + 2 = 19

57 + 2 = 59

12 + 4 = 16

32 + 34 = 66

12 + 30 = 30 + 12

+ 25 = 25 + 41

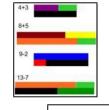
- Demonstrate the commutative law of addition
- •Re-partition numbers eg.
- Use a hundred square
- •Check calculations using inverse and by adding numbers in different order
- Using partitioning to separate tens and units, eg,

$$54 = 50 + 4$$

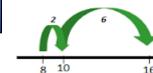
Calculations Written

Use a range of concrete and pictorial representations, including:

5555555 999999 Which line has most money? How much more? more make 10







65 = 50 + 15

65 = 40 + 25

65 = 30 + 35

65 = 20 + 45

65 = 10 + 55

Bead strings







Number tracks

Fractions

Representations to support mental and

written calculations.

Counting in fractions up to 10, starting from any numbers and using the 1/2 and 2/4 equivalence on the number line

Real everyday objects

11/4 11/4 13/4 2 21/4 21/2

•Solve problems:

- Using concrete objects, pictorial representations (numbers, quantities & measures)
- Applying increasing knowledge of mental & written methods
- •Discuss and solve problems that emphasise the value of each digit in two-digit numbers

(They should) develop the concept of addition and subtraction and ... use these operations flexibly. (Number-addition and subtraction, Non-statutory guidance.)

Links from othe strands / bar modelling

Add numbers mentally, including:

- a three-digit number and ones
- a three-digit number and tens
- a three digit number and hundreds
- Partition all numbers and recombine, start with TU + TU then HTU + TU
- Use hundred square, place value counters, number lines

Common mental calculation strategies:

Partitioning and recombining Doubles and near doubles Use number pairs to 10 and 100 Adding near multiples of ten and adjusting

Using patterns of similar calculations Using known number facts

Bridging though ten, hundred

Add numbers with up to three digits, using formal written (columnar) methods

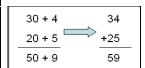
Add to three digit numbers using physical and abstract representations;

dienes, place value counters, empty number lines

Calculations Written

Calculations

Mental

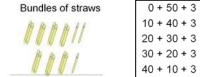


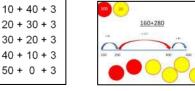
Revert to concrete representations if children find expanded/column methods difficult

What is the same and what is

different about all these methods?

Representations to support mental and written calculations.





Use a range of concrete, pictorial and abstract representations, including those below

I can explain my method using representations

Dienes and place value counters

Partitioning and recombining

= 90 + 7 = 97

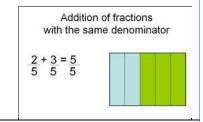
42 + 31 = 73

76 + 21

= 70 + 6 + 20 + 1

Fractions

Addition of fractions with the same denominator within one whole.



other strands, bar modelling Links from Pupils should estimate the answers to a calculation & use inverse operations to check answers. Add amounts of money using both £ and p in practical contexts.

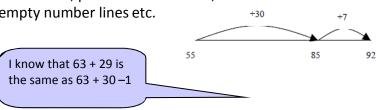
Measure, compare and add lengths (m/cm/mm), mass (kg/g) & volume/capacity (l/ml)

Use bar modelling to solve word problems - including missing number problems, using number facts, place value, and more complex addition

Informal methods to support mental Calculations

Practise mental methods with increasingly large numbers

Consolidate partitioning and re-partitioning
Use compensation for adding too much/little and adjusting
Use Dienes, place value counters,
empty number lines etc.
+30
+7



Common mental calculation strategies:

Partitioning and recombining
Doubles and near doubles
Use number pairs to 10 and 100
Adding near multiples of ten and adjusting
Using patterns of similar calculations
Using known number facts
Bridging though ten, hundred
Complementary addition

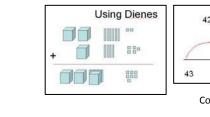
Written Calculations

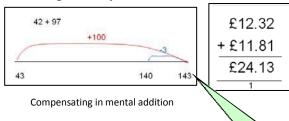
Add numbers with up to four digits, using the formal written (columnar) method Add three digit numbers using columnar method and then move onto 4 digits. Include decimal addition for money - Expanded then moving to compact

Revert to expanded methods if children find formal calculation method difficult

Representations to support mental and written calculations.

Use physical/pictorial representations alongside expanded and columnar methods.





0 + 50 + 3 10 + 40 + 3 20 + 30 + 3 30 + 20 + 3 40 + 10 + 3 50 + 0 + 3

Re-partitioning

Ask what is the same and what is different about all

these methods?

767 + 216 =

for the column

700 + 60 + 7 200 + 10 + 6

Place value cards & counters to counters, support the expanded method in readiness

70d

700 43 F

Fractions

Addition of fractions with the same denominator to become fluent through a variety of increasingly complex problems beyond one whole

Counting using simple fractions and decimals, both forwards and backwards



 $\frac{1}{2} + \frac{2}{4} = \frac{2}{4} + \frac{2}{4} = 1$

| 1/2 | 1/4 | |
|-----|-----|--|
| | 1/4 | |

Links from other strands / bar

- Estimate and use inverse operations to check answers.
- Solve addition and subtraction two step problems in context, deciding which operations and methods to use and why
- Identify, represent and estimate numbers using different representations. (Place value)
- Recognise the place value of each digit in a four-digit number.
- \bullet Estimate, compare and calculate different measures, including amounts money in £ and p (including fractions and decimals)

Informal methods to support mental Calculations

- Add numbers mentally with increasingly large numbers, e.g. 12 462 + 2300 = 14762
- Mentally add tenths, and one-digit numbers and tenths
- Add decimals, including a mix of whole numbers and decimals, decimals with different numbers of places, and complements of 1 (e.g. 0.83 + 0.17 = 1)

Children use representation of choice

Refer back to pictorial and physical representations when needed

Common mental calculations

Doubles and near doubles Adding near multiples of 10 Using patterns of similar calculations

Bridging though ten, hundred, tenth

Written

Calculations

Add whole numbers with more than four digits, using the formal written (columnar) method

Add three digit numbers using columnar method and then move onto 4 digits. Include decimal addition for money

24172m

+ 5929m 30101m £563.14 + £207.88 £771.02

Revert to expanded methods if children find formal calculation method difficult (see Y3)

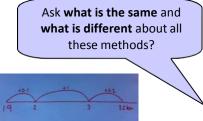
Representations to support mental and written

Use physical/pictorial representations alongside columnar methods where needed.

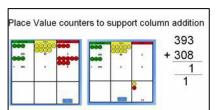
= 12 462 + 2000 + 300 = 14 462 + 300 = 14 762

12 462 + 2300

Partitioning and recombining



Jottings to support mental calculation

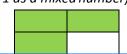


Fractions

• Add fractions with the same denominator and denominators that are multiples of the same number (to become fluent through a variety of increasingly complex problems and add fractions that exceed 1 as a mixed number)

,

Add



 $\frac{1}{2} + \frac{3}{4} = \frac{2}{4} + \frac{3}{4} = \frac{5}{4}$



Links from other strands / bar modelling

- Solve problems involving up to three decimal numbers.
- Solve addition and subtraction multi step problems in context, deciding which operations and methods to use and why
- Use all four operations to solve problems involving measure [e.g. length, mass, volume, money] using decimal notation,
- Calculate the perimeter of composite rectilinear squares in centimetres and metres
- Use angle sum facts and other properties to make deductions about missing angles
- Solve comparison, sun and difference problems using information presented in a line graph

to support menta Informal methods Calculations

• Perform mental calculations, including with mixed operations and large numbers (more complex calculations)

Children use representation of choice Consolidate partitioning and re-partitioning

Use compensation for adding too much/little and adjusting Refer back to pictorial and physical representations when needed.

Common mental calculation strategies:

Partitioning and recombining Doubles and near doubles Use number pairs to 10 and 100

Adding near multiples of ten and adjusting Using patterns of similar calculations

Using known number facts Bridging though ten, hundred, tenth Complementary addition

Calculations Written

Add larger numbers using the formal written (columnar) method

Add three digit numbers using columnar method and then move onto 4 digits.

Include decimal addition for money

£563.14 +£207.88 £771.02 111

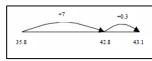
Revert to expanded methods if children find formal calculation method difficult (see Y3)

Representations to support mental and written

Use physical/pictorial representations alongside columnar methods where needed. Ask what is the same and what is different?

12 462 + 2300 = 12 462 + 2000 + 300 = 14 462 + 300 = 14 762

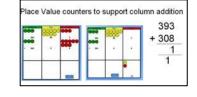




234 kg + 49 kg = 273 kg200 + 30 + 440 + 9200 + 70 + 13

I can explain my method using place value counters

What is the same and what is different about all these methods?



- Add fractions with different denominators and mixed numbers, using the concept of equivalent fractions
- Start with fractions where the denominator of one fraction is a multiple of the other (e.g. 1/2 + 1/8 = 5/8) and progress to varied and increasingly complex problems
- Practise calculations with simple fractions and decimal equivalents to aid fluency

Fractions

Links from other strands / bar

modelling

- Use their knowledge of the order of operations to carry out calculations involving the four operations (BIDMAS)
- Solve problems involving all four operations
- Algebra: use symbols and letters to represent variable and unknowns e.g. a + b = b + a
- Solve problems involving the calculation and conversions of units of measure, using decimal notation of up to three decimal places where appropriate
- Using the number line, pupils use, add and subtract positive and negative integers for measures such as temperature
- Calculate and interpret the mean as an average
- Interpret and construct pie charts and line graphs and use these to solve problems
- Find missing angles, and express geometry relationships algebraically (e.g. d=2xr)

St. John's Primary School Calculation Policy for subtraction Year 1 Subtract one digit and two-digit numbers to 20, including zero. Read, write and interpret mathematical statements using symbols (+, -, =) signs. Represent and use number bonds and related addition facts within 20 Solve one-step problems using concrete objects and pictorial representations, and missing number Calculations problems such as 7 = -9Memorise and reason with number bonds Add using objects, Numicon, cubes etc and number lines and tracks Check with everyday objects Find a 'difference' by counting up; Ensure pre-calculation steps are understood, including: Counting objects, 2 3 Conservation of number Subtract one-digit and two-digit numbers to 20, including zero. 7-3= \, 7- \, = 4 - 3 = 4, 17 - 13 = Calculations 17 - 🔲 = 4 Written Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs . What's the difference between 4 and 6? Represent and use number bonds and related subtraction facts within 20. Use a range of concrete and pictorial representations, including: Representations to support menta 1 2 3 4 5 6 7 8 9 10 and written calculations. Hands, and children Bead strings, number tracks and lines themselves. Subtraction: 000000000 Comparison Model (9) (9) (9) (9) (9) Which line has most money Peter has 5 pencils and 3 erasers. How many more pencils than erasers does he Counting in fractions to 1 Fractions $\frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = 1$ or $\frac{1}{4} + \frac{1}{4} + \frac{1}{2} = 1$ $\frac{1}{2} + \frac{1}{2} = 1$ or Pupils should combine and increase numbers, counting forwards and backwards. (They should) develop the concept of addition and subtraction and ... use these operations flexibly.

Links from other strands

bar modelling

(They should) develop the concept of addition and subtraction and ... use these operations flexibly. Problems should include the terms: put together, add, altogether, total, take away, distance between, more than and less than, so that pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

(Number-addition and subtraction, Non-statutory guidance.)

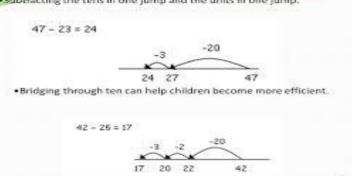
Pupils discuss and solve problems in familiar practical contexts . (*Non-statutory guidance.*) Pupils compare, describe and solve practical (measurement) problems . (*Measurement*)

Add and subtract numbers using concrete objects, pictorial representations, and mentally, including:

- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers
- adding three one-digit numbers

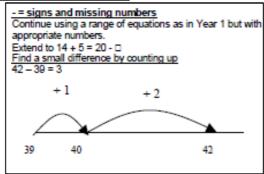
Jottings to support informal methods:

·Subtracting the tens in one jump and the units in one jump.









Calculations

Calculations

Written

Representations to support mental and

written calculations.

Mental

<u>Informal methods to support written subtraction calculations</u>

Practical portioning of a 2-digit number

In Year 1 leads to:



The difference between II and I4 is 3. I4 – II = 3

14 - 11 = 3 $11 + \square = 14$

Which line has most money?

How much more?

Rundles of straws or diones to room

600000

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Bundles of straws or dienes to represent and partition 2 digit numbers. Subtract (without decomposition) using partitioning and equipment, e.g.



To calculate 35-22, remove 22.



Then record: **35-22=13**.

Continue to use of a range of concrete and pictorial representations from Year 1—including Bar model to support understanding of **difference.** (See below.)

Fractions

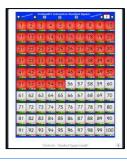
Pupils should count in fractions up to 10, starting from any number and using the equivalence on the number line (for example, 1 %, 1 %, 2 %, 2 %)

Use concrete and pictorial models of fractions to assist with counting e.g. paper cups, plates, shapes etc.

Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100.

Pupils should partition to support subtraction.

Links from other strands / I



| 55 + 45 = 100 |
|---------------|
| 45 + 55 = 100 |
| 35 + 65 = 100 |
| 100 - 55 = 45 |
| 100 - 45 = 55 |
| 100 - 35 = 65 |
| |

Solve problems with addition and subtraction:

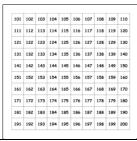
- using concrete objects and pictorial representations, involving numbers, quantities and measures
- applying knowledge of mental and written methods
- Pupils extend their understanding of the language of addition and subtraction to include sum and difference.

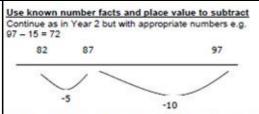
Add and subtract numbers mentally, including:

- *a three-digit number and ones
- *a three-digit number and tens
- *a three-digit number and hundreds.

Calculations

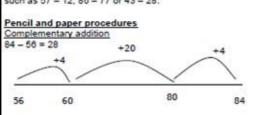
Use a number line, dienes, hundred squares, two-hundred squares, and similar representations, to support mental calculations. (See Representations section below.)





With practice, children will need to record less information and decide whether to count back or forward. It is useful to ask children whether counting up or back is the more efficient for calculations

such as 57 - 12, 86 - 77 or 43 - 28.



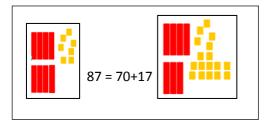
Subtract numbers with up to three digits, using formal written methods of columnar subtraction.

Written Calculations

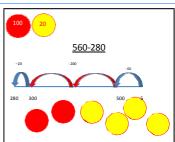
(1)Extended columnar no exchange

Extended method 87 - 53 =

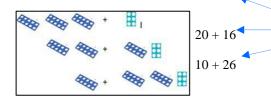
80 and 7 - 50 and 3 30 and 4 = 34 with exchange: 87-58 becomes 70 +1 7 -50 + 8 20 + 9



Representations to support mental and written calculations



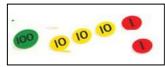
Partitioning and re- partitioning support the understanding of place-value. 30 + 6



All of these representations still comprise the amount 36

Introduce transition from concrete place value representations, (e.g. dienes) to pictorial – such as place value counters or money.





Revert to concrete and expanded methods whenever difficulties arise.

132 in dienes

132 in place value counters.

Fractions

Count up and down in tenths.

Subtract fractions with the same denominator within one whole.

Links from other strands/bar modelling

Money and calculating duration of events

For example: "Add and subtract amounts of money to give change, using both £ and p in practical contexts."

Use bar modelling to solve word problems - including missing number problems, using number facts, place value, and more complex subtractions

Continue to practise mental methods with increasingly large numbers to aid fluency. (From Non– Statutory Guidance).

Methods to support fluent calculation and encourage efficiency of method:

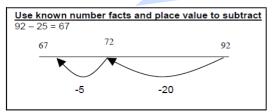
Find a small difference by counting up.

E.g. 5003-4996

- Subtract nearest multiple of ten and adjust.
- Partition larger numbers

Whenever possible, children should be encouraged to visualise number lines and other basic, supporting representations to promote fluent work with- out jottings.

This could be done using an empty number line. Children should recall and use number facts to reduce the number of steps.



Moving to

compact

methods

Add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate.

Build on formal, extended method (See Year 3) using exchange wherever necessary. Continue to use representations and manipulatives to develop understanding of place value.

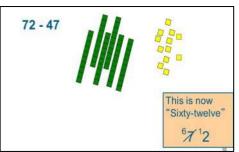
Apply understanding of subtraction with larger integers to that of decimals in context of money and measures. (See Year 5.)

Representations to support mental and written calculations

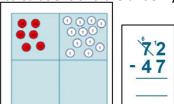
Calculations

Written Calculations

Mental



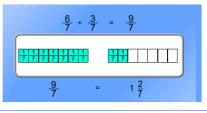
Dienes blocks or place value counters can be used to model calculations and the under-lying place value concepts.



Use physical and / or pictorial representations and expanded algorithms alongside columnar methods. Ask: What is the same? What's different? Compare and discuss the suitability of different methods in context. Pupils decide which operations and methods to use and why.

I would count on using a numberline to calculate 5003-4896 because the numbers are close together.

Fractions



Count up and down in hundredths.

Add and subtract fractions with the same denominator. Solve simple measure and money problems involving fractions and decimals to two decimal places.

Links from other

strands / bar modelling Identify, represent and estimate numbers using different representations. (*Place value*) Recognise the place value of each digit in a four-digit number.

Estimate and use inverse operations to check answers to a calculation.

Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.

Estimate, compare and calculate different measures, including money in pounds and pence.

E.g. 12 462 - 2300 = 10 162

• Use rounding to check answers to calculations In the context of a problem.

Subtract numbers mentally with large numbers

Pupils practise adding and subtracting decimals Including a mix of whole numbers and decimals with different numbers of place values and complements to 1

(for example, 1 - 0.17 = 0.83).

 Pupils mentally add and subtract tenths, and one-digit whole numbers and tenths. Find difference by counting up Partitioning Applying known facts Bridging through 10 and multiples of 10 Subtracting 9, 11 etc by compensating

Which method works best?

2

Children use, or visualise, representation of choice. Refer back to physical representations as required.

tions. See below.

Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction).

(Pupils) practise adding and subtracting decimals.

Begin with three-digit numbers using formal, columnar method; then move into four-digit numbers.

As in Year 4, compare physical and / or pictorial representations and expanded algorithms alongside columnar methods. Ask: What is the same? What's different?

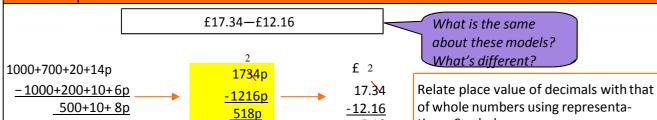
Compare and discuss the suitability of different methods, (mental or written), in context.

Revert to expanded methods whenever difficulties arise

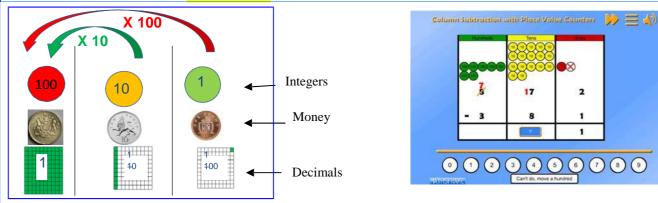
Calculations Written

Calculations

Mental



Representations to support menta and written calculations.



Use physical and pictorial representations to stress the place value relationships between money, decimals and whole numbers. A place value mat such as this one could be used, moving away from the traditional: Hundreds, tens and ones model used in Lower KS2 and KS1.

5.18

Fractions

Subtract fractions with the same denominator and denominators that are multiples of the same number. (Include fractions exceeding 1 as a mixed number.)

Solve problems involving number up to three decimal places.

They mentally add and subtract tenths, and one-digit whole numbers and tenths.

other strands/ bar modelling Links from Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign.

Use all four operations to solve problems involving time, money and measure using decimal notation.; (up to 3d.p.)

Children:

Cilliaren

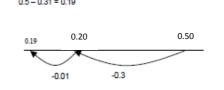
- Perform mental calculations, including with mixed operations and large numbers.
 Use estimation to check answers to calculations and determine, in the context of a problem.
- Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.
- They undertake mental calculations with increasingly large numbers and more complex calculations.

Mental Calculations

Calculations

Written

Children draw on basic, Mental subtraction Strategies, (See Year 5.) Children use, or visualise, representation of choice. Refer back to physical representations as required.



Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction). Solve problems involving the calculation and conversions of units of measure, using decimal notation of up to three decimal places where appropriate. (MEASURES)

Move towards consolidation of formal, columnar method.

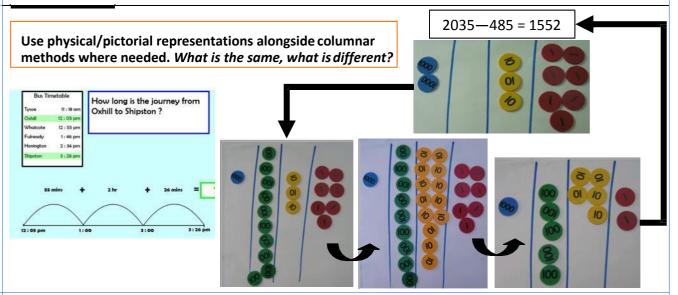
For more complex calculations, with increasingly larger or smaller numbers, compare representations and expanded algorithms alongside columnar methods. Ask: What is the same? What's different? Compare and discuss the suitability of different methods, (mental or written), in context. Revert to expanded methods whenever difficulties arise

Consolidate columnar methods, paying particular attention to the occurrence of zeros as place holders.

1 8 6 10 1₁ - 5 4 5 6 1 3 2 5 5

1 ⁷8 .90¹⁰1 ¹1
- <u>5 . 4 5 6</u>
1 2 . 5 5 5

Representations to support menta and written calculations.



 $\label{lem:Add} \textbf{Add and subtract fractions with different denominators and mixed numbers.}$

They practise calculations with simple fractions and decimal fraction equivalents to aid fluency.

Fractions

Links from other strands / bar modelling

Use their knowledge of the order of operations to carry out calculations involving the four operations (BODMAS)

Solve problems involving all four operations

Algebra: use symbols and letters to represent variable and unknowns e.g. a + b = b + aUsing the number line, pupils use, add and subtract positive and negative integers for measures such as temperature.

Calculations Mental

- · solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.
- Count in multiples of twos, fives and tens with equipment, songs & rhythms, and including by rote
 - Counting 2s e.g. counting socks, shoes, animal legs...
 - Counting in 5 s e.g. counting fingers, fingers in gloves, toes ...
 - Counting in 10s e.g. counting fingers, toes ...
- Doubles up to 10
- Recognising odd and even numbers
- Write as a number pattern (e.g. 5, 10, 15...; 2, 4, 6...; 10, 20, 30...)

What's the sequence?

> What comes next?

Calculations Written

Representations to support mental and written calculations

It is important to use a range of models to develop understanding of multiplication, and that children make connections between arrays, number patterns, and counting in twos, fives and tens

Although there is no statutory requirement for written multiplication in Year 1, it may be helpful to encourage children to begin to write it as a repeated addition sentence in preparation for Year 2

E.g. 2+2+2+2=8 or $4 \times 2=8$

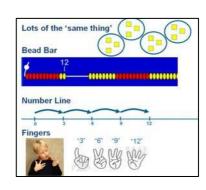
Use a range of concrete and pictorial representations, including:



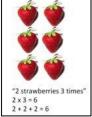


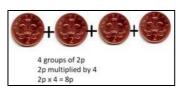




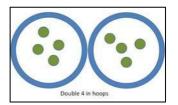


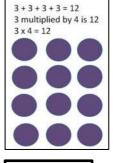














- Count in multiples of twos, fives and tens (from Number and place value), as above
- Counting in twos, five and tens from different multiples to develop their recognition of patterns in the number system
- They discuss and solve problems in familiar practical contexts, including using quantities.
 - Using bar modelling to solve simple problems how many sweets in 5 bags?

Links from other strands / bar modelling

- Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, connecting the 2, 5 and 10 multiplication tables to each other
- Connect the 10 multiplication table to place value
- Recognise odd and even numbers
- show that multiplication of two numbers can be done in any order (commutative)
- Use a variety of language to describe multiplication and division
- Apply doubling of numbers up to ten to doubling larger numbers
- Counting in 3s odd / even pattern

I know that the multiples of 2/5/10 are always / never

Written Calculations

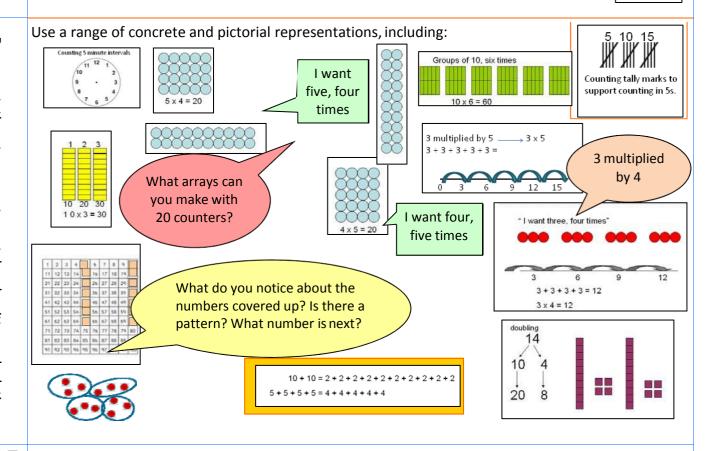
Calculations

Mental

- calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (x), division (÷) and equals (=) signs
- Begin to use other multiplication tables and recall facts to perform written calculations
- Use a range of materials and contexts ... including arrays and repeated addition

 $7 \times 2 = \square$ $7 \times \square = 14$ $\square \times 2 = 14$ $\triangle \times \square = 14$

Representations to support mental and written calculations



Fractions

- write simple fractions for example, 1/2 of 6 = 3 and recognise the equivalence of 2/4 and 1/2
- Begin to relate multiplication and division models to fractions and measures

Links from other strands / bar

modelling

- solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.
- Use commutativity and inverse relations to develop multiplicative reasoning (e.g. $4 \times 5 = 20$ and $20 \div 5 = 4$)
- Statistics—interpret and construct simple pictograms, tally charts and block diagrams
- Measurement— counting 5 minute intervals on a clockface
- Place value count in steps of 2, 3 and 5 from 0 and in tens from any number, forwards and backwards

- recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables (and 2, 5 and 10 multiplication tables from Y2)
- Use doubling to connect 2, 4 and 8 multiplication tables
- Develop efficient mental methods using commutativity and associativity
- Derive related multiplication and division facts
- calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental methods

 The commutative law:
- Partitioning: multiply the tens first and then multiply the units,
 e.g. 57 x 6 = (50 x 6) + (7 x 6) = 300 + 42 = 342
- Children can apply these skills to solve spoken word problems too,
- Include missing number statements e.g 72 ÷ = 8

Ensure opportunities to learn multiplication tables through use of visual models, images and also rote learning.

Multiplication and division facts: 8 x 4 = 32, 4 x 8 = 32, 32 ÷ 4 = 8, 32 ÷ 8 = 4 I have 8 packets, each containing 12 crayons. How many crayons do

I have in total?'

Deriving related facts: $3 \times 2 = 60, 6 \div 3 = 2, 6 \div 2 = 3$ $3 \times 2 = 60, 60 \div 3 = 20, 20 = 60 \div 3$

 $4 \times 12 \times 5 = 4 \times 5 12$

 $4 \times 12 = 12 \times 4$

 $= 20 \times 12$

= 240

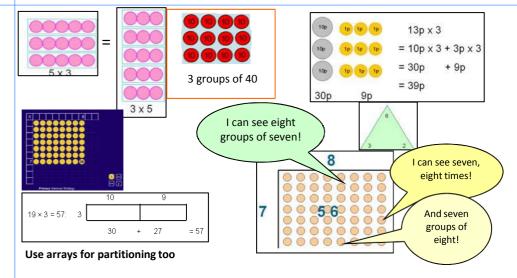
Written Calculations

Calculations

Mental

- write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers,
- progressing to formal written methodsEstimate before calculating
- Ensure written methods build on/relate to mental methods

Representations to support mental and written calculations.



2 digit x 1 digit number:
e.g. 7 x 38 = 266

x 30 8
7 210 56
210 + 56 = 266

Tm 2 times as tall as you.

I'm 3 merrer tall.

I'm only i metrer tall.

Three times as many i as many in a many i as many in a many i as many i a

Fractions

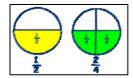
recognise and show, using diagrams, equivalent fractions with small denominators

 2
 4
 6
 8
 10
 12
 14
 16
 18
 20

 3
 6
 9
 12
 15
 18
 21
 24
 27
 30

 4
 8
 12
 16
 20
 24
 28
 32
 36
 40

 5
 10
 15
 20
 25
 30
 35
 40
 45
 50



Links from other strands / bar modelling

- The comparison of measures includes simple scaling by integers (for example, a given quantity or measure is twice as long or five times as high)
- Pupils now use multiples of 2, 3, 4, 5, 8, 10, 50 and 100.
- Pupils understand and use simple scales (for example, 2, 5, 10 units per cm) in pictograms and bar charts with increasing accuracy
- solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

to support menta Informal methods Calculations

Calculations

Written

- recall multiplication and division facts for multiplication tables up to 12 × 12
- use place value, known and derived facts to multiply and divide mentally, including:
 - multiplying by 0 and 1;
 - dividing by 1;
 - multiplying together three numbers
- recognise and use factor pairs and commutativity in mental calculations
- practise mental methods and extend this to three-digit numbers to derive facts, (for example $600 \div 3 = 200$ can be derived from $2 \times 3 = 6$)

Using the **distributive** law: $39 \times 7 = 30 \times 7 + 9 \times 7$

Using the **associative** law: $(2 \times 3) \times 4 = 2 \times (3 \times 4)$

> Using facts and rules: $2 \times 6 \times 5 = 10 \times 6 = 60$

multiply two-digit and three-digit numbers by a one-digit number using formal written layout

- Estimate before calculating
- Ensure written methods build on/relate to mental methods

(e.g. grid method) Introduce alongside grid and expanded column methods

54 50 X 4 16 16 (4 x 4) <u> 200</u> (50×4) 216

Key skills to support:

- •know or quickly recall multiplication facts up to 12 × 12
- understand the effect of multiplying
- numbers by 10, 100 or 1000 •multiply multiples of 10, for example, 20
- •approximate, e.g. recognise that 72 × 38 is approximately $70 \times 40 = 2800$ and use this information to check whether their answer appears sensible

Revert to expanded methods if children find formal calculation method difficult

Moving digits ITP

2 0 4 8 5

00233567

2 0 4 8 5

Representations to support menta and written calculations

Ensure children can confidently multi- ply & divide by 10 and 100, that multiplying by 10 makes the number bigger and all digits move one place to the left, while dividing by 10 makes the number smaller and all the digits move one place to the right.

Use arrays made with place value counters to demonstrate the link between multi- plication and division. This will support understanding of the grid 120 method.

Children need to understand and apply the language of multiples and factors and use it in solving multiplication and division problems, for example, 'All factors of 36 are multiples of 2, true or false? Find me two factors of 48 that are also

This digit is

worth 200

245 This digit is 6 worth 30 I can use place value counters to model the grid method 0000 000

recognise and show, using diagrams, families of common equivalent fractions

• understand the relation between non-unit fractions and multiplication and division of quantities, with particular emphasis on tenths and hundredths.

multiples of 3.'

 make connections between fractions of a length, of a shape and as a representation of one whole or set of quantities.

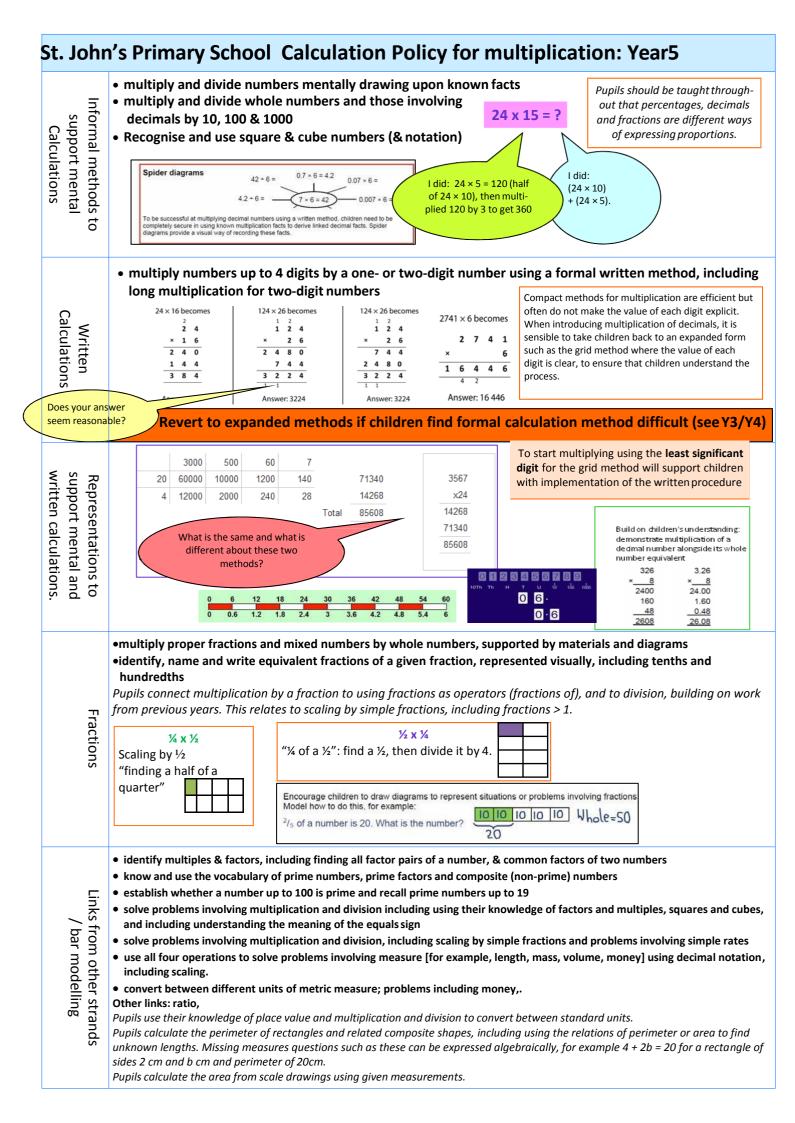
• use factors and multiples to recognise equivalent fractions and simplify where appropriate

<u>10</u> <u>15</u> 20 25 30 35 40 40

- · solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.
- Convert between different units of measure (e.g. km to m) use multiplication to convert from larger to smaller units
- Understand the relation between non-unit fractions and multiplication/division of quantities. With particular emphasis on tenths and hundredths
- relate area to arrays and multiplication.
- Problem solving work can involve finding all possibilities and combinations drawing on knowledge of multiplication tables facts
- Pupils understand and use a greater range of scales in their representations (Statistics)

strands / bar modelling Links from other

Fractions



Informal methods to support mental Calculations

 perform mental calculations, including with mixed operations and large numbers (increasingly large numbers & more complex calculations)

- use all the multiplication tables to calculate mathematical statements in order to maintain fluency.
- •use estimation to check answers to calculations & determine, in the context of a problem, an appropriate degree of accuracy.
- •identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places.

Children should know the square numbers up to 12 × 12 & derive the corresponding squares

of multiples of 10 e.g. $80 \times 80 = 6400$

Use mental strategies to solve problems e.g.

- x4 by doubling and doubling again
- x5 by x10 and halving
- x20 by x10 and doubling
- x9 by multiplying by 10 and adjusting
- x6 by multiplying by 3 and doubling

How many different x/÷ facts can you make using 72? 7.2? 0.72?

What is the best approximation for 4.4 x 18.6?

Written Calculations

support mental and written calculations

- multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication (short & long multiplication)
- multiply one-digit numbers with up to two decimal places by whole numbers

£ 6.23 x 27 43.61 124.60 £ 168.21

Revert to expanded methods if children find formal calculation method difficult (see Y4/Y5)

Look at long-multiplication calculations containing errors, identify the errors and determine how they should be corrected

a × 3 b + 7 14.5

 X
 8
 0.4
 0.06

 11
 88
 4.4
 0.66
 = 93.06

 What's the same?
 What's different?

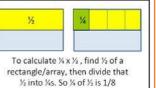
•multiply simple pairs of proper fractions, writing the answer in its simplest form e.g. $\frac{1}{2}$ x $\frac{1}{2}$ = 1/8

Fraction

Representations to

Three key applications of understanding:

- Recognise that ¼ of 12, ¼ x 12 and 12 divided by 4 are equivalent
- •Use cancellation to simplify the product of a fraction and an integer e.g. ½ x 15 = 3, ½ x 15 = 2 x ½ x 15 = 2x3 = 6
- •Work out how many ½s in 15, how many ¾s in 15, how many 2/5s in 1 etc.



Pupils should use a variety of images to support their understanding of multiplication with fractions. This follows earlier work about fractions as operators (fractions of), as numbers, and as equal parts of objects, e.g. as parts of a rectangle.

•identify common factors, common multiples and prime numbers

- use their knowledge of the order of operations to carry out calculations involving the four operations
- solve problems involving addition, subtraction, multiplication and division
- explore the order of operations using brackets; for example, $2 + 1 \times 3 = 5$ and $(2 + 1) \times 3 = 9$.
- Fractions, decimals and percentages including equivalences in different contexts.
- solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts
- solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison
- solve problems involving similar shapes where the scale factor is known or can be found
- solve problems involving unequal sharing and grouping using knowledge of fractions and multiples.
- •Algebra including formulae, linear number sequences, combinations of variables
- •Measurement including solving problems with conversion of units, decimal notation, area & volume
- •Statistics including pie charts, line charts and calculating the mean

Links from other strands
/ bar modelling

Mental Calculations

Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. (Pupils) make connections between arrays, number patterns, and counting in twos, fives and tens.



Pictorial jottings to

Count on or back in 2s, 5s and 10s and useful look for patterns.



support the calculation of 8 ÷ 4

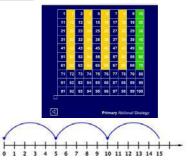
Written

Calculations

userui look foi patterns.

Children should experiment with the concepts of sharing and grouping in a number of contexts. Initially they use their own recording—moving towards fluent, symbolic notation in Year 2.

Conceptual understanding and recording should be continuously supported by the use of **arrays** as a default model, as well as other representations, (see below.)



The relationship between multiplication and division must be continually considered.

Use a range of concrete and pictorial representations, including:

• Manipulatives to support children's own recording; and understanding of *sharing* and the link with multiplication.

"How can we share 6 cakes between 3 people?



Here, the cakes are placed in an array formation.

How many 2 tiles can we fit on the 6 tile?

Bead strings

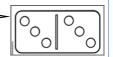
Moving from concrete to pictorial, counters to represent the cakes to reinforce the relationship between multiplication and division.

• Manipulatives, and real-life objects to support children's own recording; and understanding of *grouping* and the link with multiplication.



Coat hangers and socks support calculation of 8÷2

"Double 3 is 6. Half of 6 is 3."



• Dominoes and dice to reinforce concepts of doubling and halving.

Recognise, find and name a half as one of two equal parts of an object, shape or quantity Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity. (See Representations above.)

Fractions

Representations to support mental and written

calculations.

They practise counting as reciting numbers and counting as enumerating objects, and counting in twos, fives and tens from different multiples to develop their recognition of patterns in the number system (for example, odd and even numbers). (PLACE VALUE).

Pupils are taught half and quarter as 'fractions of' by solving problems using shapes, objects and quantities. (FRACTIONS)

Links from other strands bar modelling

Division and multiplication concepts must be linked continuously.

Mental Calculations

The relationship between multiplication and division must be continually considered

- Recall and use multiplication and division facts for the 2, 5, 10, 3s multiplication tables, including recognising odd and even numbers .
- Calculate mathematical statements for multiplication and division within
- the multiplication tables and write them using the multiplication (x) division (±) and equals (=) signs

"5, one time", "5, two times" and so on.





Written Calculations

- Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot
- Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts. (See below.)



Pupils decode a problem first, represent it using manipulatives and jottings; and finally record it symbolically.

Representations to support menta and written calculations.

Use a range of concrete and pictorial representations, including:

66

66

Arrays



7 x 2 = 14



 $2 \times 7 = 14$ $14 \div 7 = 2$ Is 14 an odd number? How do you know?



Number lines to support grouping



10p + 10p + 10p + 10p + 10p = 50p $10p \times 5 = 50p$ 5 hops of 10

How many groups of 5 minutes have passed when the minute

Representations to support multiplicative reasoning:



Using Dienes: "If 40 ÷ 10 = 4 and 30 ÷ 10 = 3, what do you think 70 ÷ 10 would be? Why?"

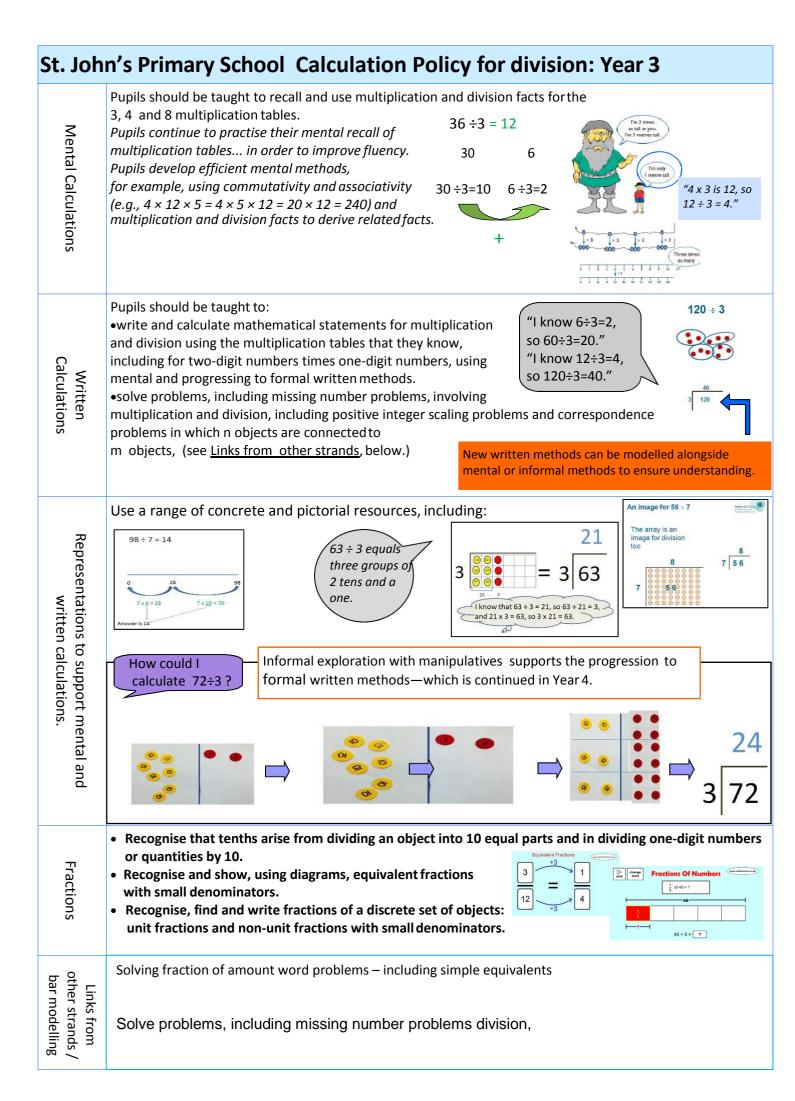


Fractions

Recognise, find, name and write fractions $\frac{1}{2}$, $\frac{1}{4}$, $\frac{3}{4}$, $\frac{2}{4}$ of a length, shape, set of objects or quantity Write simple fractions for example, $\frac{1}{2}$ of 6 = 3 and recognise the equivalence of $\frac{1}{2}$ and $\frac{2}{4}$.

Links from other strands bar modelling

- Count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward.
- Recognise the place value of each digit in a two-digit number (tens, ones) (PLACE VALUE).
- Tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times, (MEASURES).



Informal methods to support mental Calculations

Pupils should be taught to:

- recall multiplication and division facts for multiplication tables up to 12 × 12
- use place value, known and derived facts to multiply and divide mentally,

including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers

· recognise and use factor pairs and commutativity in mental calculations

Using known facts and blank arrays to calculate 176÷8.

Pupils practise mental methods and extend this to three-digit numbers to derive facts.

Written Calculations

Pupils should be taught to:

• solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.

Pupils practise to become fluent in the formal written method of short multiplication and short division with exact answers .

Revert to expanded methods if children find formal calculation method difficult

Representations to support mental and written calculations.

By working through larger number calculations with manipulatives, children gain experience of exchange (re-partitioning) within division algorithms.

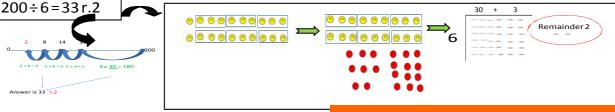
492÷4 1 2 3

I know that

 $6 \div 3 = 2$, so

600÷3=

By the end of Year 4, children need to have encountered remainders in a number of contexts. Pupils can be introduced to remainders using known facts: e.g. 13÷4; and then progress to larger numbers. (See below).



Money can be used instead of place value counters.

Fractions

Pupils should be taught to:

manipulatives into 3 rows), child

B checks it and records this in a

formal, short division format.

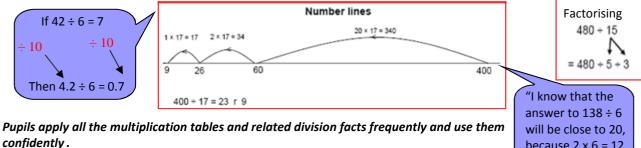
- recognise and show, using diagrams, families of common equivalent fractions
- recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten.
- solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number
- find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths
- Convert between different units of measure [for example, kilometre to metre; hour to minute]
- Estimate, compare and calculate different measures, including money in pounds and pence (MEASURES)
- Recognise that hundreths arise when dividing an object by one hundred and dividing tenths by ten. (FRACTIONS)

Links from othe strands / bar modelling

Informal methods to support mental Calculations

- . Pupils should be taught to:
- multiply and divide whole numbers and those involving decimals by 10, 100 and 1000
- multiply and divide numbers mentally drawing upon known facts

identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers .



confidently.

because $2 \times 6 = 12$, so 20 x 6 = 120."

Calculations

Written

Pupils practise and extend their use of the formal written methods of short multiplication and short division.

Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and

interpret remainders appropriately for the context.

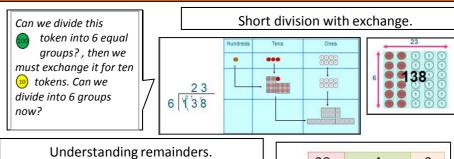
98 + 7 becomes 432 ÷ 5 becomes

5 r1

Pupils interpret non-integer answers to division by expressing results in different ways according to the context, including with remainders, as fractions, as decimals or by rounding. (See Representations below.)

Revert to expanded methods if children find formal calculation method difficult

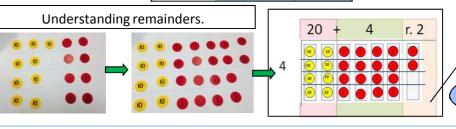
Representations to support menta and written calculations.



Practical experience with manipulatives is vital for children to talk through the language of division e.g. exchange, remainder; and to embed conceptual understanding.

2 out of a whole group of $4 = \underline{2} = \underline{1} = 0.5$

4 2



 $98 + 4 = \frac{98}{4} = 24 \cdot 2 = 24 \cdot \frac{1}{2} = 24.5$ What is the same? What's different about the ways that these remainders are expressed?

Fractions

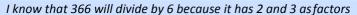
- Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number .
- Pupils connect equivalent fractions > 1 that simplify to integers with division and other fractions > 1 to division with
- Pupils connect multiplication by a fraction to using fractions as operators (fractions of), and to division.
- Pupils should make connections between percentages, fractions and decimals

Links from other strands bar modelling

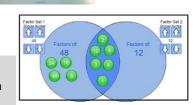
- Pupils use all four operations in problems involving time and money, including conversions.using decimal notation, including scaling.
- calculate and compare the area of rectangles (including squares). (MEASURES)
 - establish whether a number up to 100 is prime and recall prime numbers up to 19
 - recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3)
 - solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes and including scaling by simple fractions and problems involving simple rates.
 - solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign. (NUMBER-MULTIPLICATION AND DIVISION)

Pupils should be taught to:

- perform mental calculations, including with mixed operations and large numbers.
- use their knowledge of the order of operations to carry out calculations involving the four operations.
- identify common factors, common multiples and prime numbers.



- Solve problems involving addition, subtraction, multiplication and division
- use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.

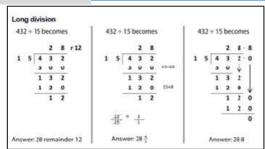


Written Calculations

informal methods to support

mental Calculations

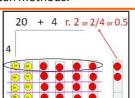
- divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context
- divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.
- Pupils practise division for larger numbers, using the formal written methods of short and long division.



Representations to support mental and written calculations.

Representations to s Representations to s

To introduce the long division model, use a calculation which can be represented both with manipulatives and by a short division algorithm. Use questioning and discussion to compare written methods.



Revert to expanded methods if children find formal calculation method difficult

2 4 r.2 4 9 18 - 8 0 (4 x 20) 1 8 - 1 6 (4 x 4) 2 What's the same? What's different?

Fractions

use common factors to simplify fractions,

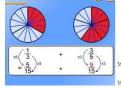
£1362.72 ÷ 4 = £340.68

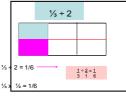
£340.68 ÷ 10 = £34.068

which rounds to £34.07

[½ and ½ again.]

- •compare and order fractions, including fractions > 1
- add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions
- •divide proper fractions by whole numbers [for example, $1/3 \div 2 = 1/6$ and by fractions $-2/3 \div 1/3$





- •associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375.]
- Pupils use their understanding of the relationship between unit fractions and division to work backwards
 Use written division methods in cases where the answer has up to 2 dp.
 Multiply mixed number fractions 2 ½ x 4

Links from other strands

- Pupils are introduced to the division of decimal numbers by one-digit whole number, initially, in practical contexts involving measures and money. They recognise division as the inverse of multiplication.

 **S is the best estimate for 72.34 ÷ 8.91; because the numbers in the algorithm*
- Pupils also develop their skills of rounding and estimating. This includes \(\sum \) can be rounded to 72 ÷ 9."
 rounding answers to a specified degree of accuracy and checking the reasonableness of their answers. (FRACTIONS)
- solve problems involving the calculation and conversion of units of measure, using decimal notation up to three decimal places where appropriate.
- use, read, write and convert between standard units....using decimal notation to up to 3d.p. (MEASURES)
- interpret and construct pie charts and line graphs and use these to solve problems
- calculate and interpret the mean as an average. (STATISTICS)
- solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts (RATIO AND PROPORTION)

| Calculation Policy References | | | | |
|---------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|--|
| Addition | Number track <u>www.sparklebox.co.uk</u> (Year 1) Straw bundles image <u>www.idoradesign.blogspot.com</u> (Years 1 and 2) Addition with place value counters http://mathsframe.co.uk/en/resources/resource/241/ Expanded Addition using Place Value Counters (Year 5) | | | |
| Subtraction | Interactive hundred square http://www.crickweb.co.uk/ks1numeracy.html (Year 2, subtraction) http://langfordmath.com/ECEMath/BasicFacts/CuisenaireAddSubText.html: http://mathsframe.co.uk/en/resources/resource/242/ | | | |
| Multiplication | Mumsnet.com Socks image www.boden.co.uk (Year 1) ITP Multiplication array http://www.teachfind.com/national-strategies/mathematics-itp-multiplication-array (Year 3) Moving digits ITP http://www.taw.org.uk/lic/itp/mov digits.html (Years 4 and 5) Function machine ITP http://mathsframe.co.uk/en/resources/resource/70/itp function machine (Year 6) | | | |
| Division | Socks image http://www.comparestoreprices.co.uk/dolls/zapf-creation-baby-annabell-2-pairs-of-socks-759950asp (year 1) Counting by 2 song http://www.youtube.com/watch?v=hae10bsW CM (Year 1) Domino doubles www.yescoloring.com (Year 1) Division triangles http://www.topmarks.co.uk/Flash.aspx?f=triangularcardsv4 (Year 2) Clock face www.wyzant.com (Year 2) http://www.cimt.plymouth.ac.uk/projects/mepres/primary/pb3b 2.pdf (Links from other strands year 3) Fractions http://mathsframe.co.uk/en/resources/resource/144/fractions of numbers (Year 3) Arrays, Multiplication and Division article by Jennie Pennant http://nrich.maths.org/8773 (Year 4) Fractions ITP http://www.taw.org.uk/lic/itp/fractions.html (Year 4) Adding and Subtracting Fractions www.mathsframe.co.uk (Year 6, fractions) Factors www.teacherled.com (Year 6) | | | |
| Additional Materials used throughout: | DfE Models and images for understanding and manipulating numbers in Years 1 to 3 (2003) DCSF Overcoming Barriers in Mathematics (2007) Crown Copyright; materials from CD-Roms NCETM, images to support the teaching of the 4 operations from PD Lead Support Programme training 'Thinking blocks' – website and ipad app for bar modelling, fractions and word problems Mathinenglish – for missing digits in long multiplication and long division | | | |